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## Problem A. Huge Table

Input file: `stdin`  
Output file: `stdout`  
Time limit: 2 seconds  
Memory limit: 256 megabytes

We have a rectangular table consisting  $2^n$  rows and  $2^m$  columns. The integer numbers are written from left to right, from top to bottom, in the cells of table. for an instance, when  $n = 2$  and  $m = 3$ , our table is like this:

1	2	3	4	5	6	7	8
9	10	11	12	13	14	15	16
17	18	19	20	21	22	23	24
25	26	27	28	29	30	31	32

For convenience of presentation we use the notation  $[r, c]$  to denote a cell of table.  $V[r, c]$  is the number written in  $[r, c]$ .

Let's define three functions:

- $popcount(n)$  is sum of digits in the binary representation of  $n$ .  $n$  should be non-negative. For example  $popcount(7) = 3$  and  $popcount(10) = 2$ .
- $minpath(r, c)$ : Consider a sub-rectangle of our table that  $[1, 1]$  is its top-left corner and  $[r, c]$  is its right-bottom. We want to go from  $[1, 1]$  to  $[r, c]$  and in each step we are just allowed to move one cell right or down. For each cell  $[x, y]$  there is an entrance cost which is equal to  $popcount(V[x, y])$ . The function  $minpath(r, c)$  calculates the minimum cost we should pay to reach from  $[1, 1]$  to  $[r, c]$ .
- $sum(r_1, c_1, r_2, c_2)$  calculates  $\sum popcount(V[r, c])$  for all cells like  $[r, c]$  that lie in the sub-rectangle described by  $[r_1, c_1]$  and  $[r_2, c_2]$ . Formally  $(r_1 \leq r \leq r_2, c_1 \leq c \leq c_2)$ .

Now you should find answer of the following interesting queries:

1. MINPATH  $r$   $c$ : Print  $minpath(r, c)$
2. SUM  $r_1$   $c_1$   $r_2$   $c_2$ : Print  $sum(r_1, c_1, r_2, c_2)$

### Input

There are three integers in the first line:  $n$ ,  $m$  and  $q$  ( $0 \leq n \leq 50, 0 \leq m \leq 50, 1 \leq q \leq 100$ ).

The next  $q$  lines contain the queries in the format, given in the statement.

For MINPATH queries:  $(1 \leq r \leq 2^n, 1 \leq c \leq 2^m)$  For SUM queries:  $(1 \leq r_1 \leq r_2 \leq 2^n, 1 \leq c_1 \leq c_2 \leq 2^m)$

### Output

For each query, output a single integer in a line corresponding to the answer of each query. Answers may become very large, so output them modulo 1000000009.

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## Examples

stdin	stdout
2 3 5	1
MINPATH 1 1	20
SUM 2 2 3 5	9
MINPATH 3 3	81
SUM 1 1 4 8	24
MINPATH 4 7	

## Note

For the last query of the first sample “ MINPATH 4 7 ”, we can move in the following path:

$[1, 1] \rightarrow [1, 2] \rightarrow [1, 3] \rightarrow [1, 4] \rightarrow [2, 4] \rightarrow [3, 4] \rightarrow [3, 5] \rightarrow [3, 6] \rightarrow [4, 6] \rightarrow [4, 7]$

Cost of the path is:  $popcount(1) + popcount(2) + popcount(3) + popcount(4) + popcount(12) + popcount(20) + popcount(21) + popcount(22) + popcount(30) + popcount(31) = 1 + 1 + 2 + 1 + 2 + 2 + 3 + 3 + 4 + 5 = 24$